

1 Thermal conductivity of unfrozen and partially frozen managed peat soils

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10

## 11 Abstract

12

13 Detailed, accurate information on soil temperature is crucial for understanding processes leading  
14 to solute leaching and greenhouse gas (GHG) emissions from managed peat soils, but few studies  
15 have attempted to study these processes in detail. Drained peat soils have different characteristics  
16 from pristine peat. Cultivated peat soils, in particular, have high mineral matter content in the  
17 plough layer, due to mineralisation of peat and, sometimes, addition of mineral material. This  
18 study examined the effect of mineral matter content on thermal conductivity ( $\lambda$ ) in partially  
19 frozen and unfrozen peat samples. Effect of change in temperature from  $-3^{\circ}\text{C}$  to  $-10^{\circ}\text{C}$  on thermal  
20 conductivity was also estimated. Three existing models for estimating the thermal conductivity  
21 of organic soils were assessed for their suitability for cultivated drained peat soils. The thermal  
22 conductivity of peat samples with three different levels of mineral matter content was  
23 determined, using the single probe method, in the saturated state and when subjected to at least  
24 two different matric potentials at five different temperatures ( $+10^{\circ}\text{C}$ ,  $+1^{\circ}\text{C}$ ,  $-3^{\circ}\text{C}$ ,  $-5^{\circ}\text{C}$  and  $-$   
25  $10^{\circ}\text{C}$ ). The results showed that  $\lambda$  values differed between peat soils depending on mineral matter  
26 content, ice content and moisture content. The samples with the highest mineral matter content  
27 and bulk density had higher thermal conductivity at positive temperatures and to a lesser extent,  
28 at freezing temperatures, when volumetric water content and volume of water-free pores was  
29 similar. Most soil samples, especially those with no added mineral soil, were not fully frozen at  
30  $-3^{\circ}\text{C}$  and  $-5^{\circ}\text{C}$ , but this had minor effect on thermal conductivity compared with values measured  
31 at  $-10^{\circ}\text{C}$ . The Brovka-Rovdan model proved reasonably good at predicting frozen thermal  
32 conductivity in sand-enriched peat soils, while the de Vries model proved best at estimating  
33 thermal conductivity for unfrozen peat samples. We provide a first estimate of the thermal  
34 conductivity of (partially) frozen cultivated peat measured using undisturbed samples. These

35 results can be used to parameterise numerical heat transport models for simulating soil processes  
36 and GHG emissions.

37

### 38 **Abbreviations**

39 VWC = volumetric water content of the soil ( $\text{m}^3 \text{m}^{-3}$ )

40 VWPS = water-filled pore space ( $\text{m}^3 \text{m}^{-3}$ )

41 VAC = volumetric air content of the soil ( $\text{m}^3 \text{m}^{-3}$ )

42 VIC = volumetric ice content of the soil ( $\text{m}^3 \text{m}^{-3}$ )

43 OM = organic matter content ( $\text{g g}^{-1}$ )

44 BD = bulk density ( $\text{g cm}^{-3}$ )

45  $\lambda$  = thermal conductivity

46 von Post scale = degree of humification according to the von Post classification system

47 L = peat samples with low mineral matter content,

48 M = peat samples with medium mineral content (plough layer of a cultivated peatland site)

49 H = manufactured peat samples with high mineral matter content

## 50 **1. Introduction**

51 Soil thermal conductivity ( $\lambda$ ) is a critical parameter controlling soil temperature. It is therefore  
52 important to understand variations in thermal conductivity when dealing with temperature  
53 regulated soil processes such as decomposition (e.g. Fang and Moncrieff, 2001), nutrient  
54 leaching (e.g. Jabloun et al., 2015) and production of greenhouse gases (GHG) (e.g. Schaufler et  
55 al., 2010). Land use and management alter peat soil properties, including thermal properties.  
56 Drainage increases decomposition rates leading to lower porosity in most peat soils, and  
57 cultivation practices further intensify this process (e.g. McLay et al., 1992, Kechavarzi et al.,  
58 2010). Moreover, some cultivated peat soils have a high mineral matter content in the plough  
59 layer due to deliberate addition of mineral soil as an amendment (Myllys and Soini, 2008). There  
60 have been some studies on thermal conductivity in peat samples from pristine mires (e.g.  
61 Kettridge and Baird, 2007, Hamamoto et al., 2010, Smerdon and Mendoza, 2010), but not in  
62 undisturbed cultivated peat. Moreover, only Konovalov and Roman (1973) and Brovka and  
63 Rovdan (1999) have studied the effect of mineral soil inclusion on peat thermal conductivity.  
64 There is thus a need for more studies on the effect of changes in peat physical properties on soil  
65 thermal conductivity.

66 In theory, the thermal conductivity of soils is most strongly controlled by the relative  
67 fraction of water, ice and air content, as thermal conductivity is much higher for water than for  
68 air (de Vries, 1963). Previous studies have found that soil thermal conductivity increases with  
69 water content in both mineral and organic soils (e.g. de Vries, 1963). The increase has been found  
70 to be almost linear in peat soils (Konovalov and Roman, 1973, Kujala et al., 2008, O'Donnell et  
71 al., 2009, Hamamoto et al., 2010, Dissanayaka et al., 2012), although some studies suggest an  
72 exponential relationship for peat (Côté and Konrad, 2005). On the other hand, soil thermal  
73 conductivity is inversely correlated with air-filled porosity (Ochsner et al., 2001). In addition to  
74 water, ice and air content, mineral matter content and organic matter content (OM) are usually

75 the key factors influencing soil thermal properties, their relative importance depending on  
76 circumstances. In organic soils, the thermal conductivity is typically lower than that in mineral  
77 soils (especially soils with quartz minerals) and has generally been found to increase with  
78 increasing mineral matter content (Brovka and Rovdan, 1999).

79 Thermal conductivity of water-saturated frozen peat is close to that of ice and higher  
80 than that of an unfrozen soil. In general, thermal conductivity does not change significantly with  
81 temperature if the soil (peat or mineral) remains either fully unfrozen or fully frozen (e.g.  
82 Campbell and Norman, 1998). However, less is known about the thermal conductivity of peat  
83 soil that is only partially frozen. Such knowledge is needed as frozen conditions or freezing-  
84 thawing processes are important for e.g. estimating GHG production in peatlands. In previous  
85 studies on frozen peat soils (Brovka and Rovdan, 1999, Kujala et al., 2008), thermal conductivity  
86 has been measured only at a temperatures lower than  $-10^{\circ}\text{C}$ , representing totally frozen  
87 conditions. Lack of studies at a range of sub-zero temperatures creates problems for accurate  
88 modelling of peat soils at negative temperatures close to  $0^{\circ}\text{C}$ , due to the fact that peat only starts  
89 to freeze at temperatures lower than  $-2^{\circ}\text{C}$  and may not be fully frozen even at  $-5^{\circ}\text{C}$  (Konovalov  
90 and Roman, 1973, Smerdon and Mendoza, 2010).

91 In this study, thermal conductivity was examined at five different temperatures (T)  
92 ranging from  $+10^{\circ}\text{C}$  to  $-10^{\circ}\text{C}$  including partly frozen conditions ( $T = -3^{\circ}\text{C}$  and  $-5^{\circ}\text{C}$ ) in a  
93 laboratory setting. Furthermore, samples with differing mineral matter content representing  
94 different cultivated peat soils, and subjected to different soil matric potentials, representing  
95 different water drainage depths, were tested. The research questions were: I) Does high mineral  
96 matter content, often observed for cultivated peat soil, result in substantially different thermal  
97 conductivity compared to other drained peat soil? II) Does the ice content in peat increase with  
98 decreasing temperature from  $-3^{\circ}\text{C}$  to  $-10^{\circ}\text{C}$  so much that the thermal conductivity substantially  
99 increases? III) Which of the three empirical thermal conductivity models tested is best for

100 estimating the thermal conductivity of peat soils with different mineral matter contents (in frozen  
101 and unfrozen state)?

102

## 103 **2. Materials and methods**

### 104 **1.1 Study sites**

105 The samples used in this study were boreal fen peat collected from the partly drained Pelso  
106 peatland complex in Northern Finland, which comprises a cultivated peatland area, a peatland  
107 forest and a peat extraction site (see Mustamo et al., 2016 for detailed description). The thermal  
108 conductivity models were also tested with undisturbed samples from two depths (10-20 cm and  
109 30-40 cm) of two cultivated peatland sites, Majnegården and Örke, in Sweden (see Berglund and  
110 Berglund, 2011 for further details of these sites.) These additional samples were included to  
111 increase the generalisability of the model test results by adding variety to physical properties of  
112 the samples (while keeping manipulation of samples to a minimum).

113           The cultivated peat at Pelso was first drained in the 1930s and since then the field has  
114 been under a rotation with timothy grass (*Phleum pratense*) for 3-4 years, followed by one year  
115 of barley (*Hordeum vulgare*). Mineral soil and lime have been mixed into the topsoil of the peat  
116 (mainly *Carex* peat) since initial drainage, to enhance the cultivation properties. Chemical  
117 fertiliser has also been regularly applied at the site. Mean groundwater depth during the growing  
118 season of 2012 was 40-65 cm below peat surface, depending on the location of measurement.  
119 The forest site is inefficiently drained (mean groundwater depth during the growing season of  
120 2012 was 16-22 cm below soil surface), resulting in ponding water in some places. Partly for  
121 this reason, the forest is a poorly growing dwarf shrub-type forest that has not been fertilised or  
122 limed since drainage in the 1970s. The main peat type is *Carex* at the forest site. The peat  
123 extraction site was a former peatland forest (similar to that described above), which was drained  
124 in 2006 and the uppermost peat layer removed. The remaining peat is mostly *Carex* mixed with  
125 *Sphagnum* peat at this site. Mean groundwater depth during the growing season of 2012 was 67  
126 cm below peat surface at the peat extraction site.

127           The Majnegården site has been used for grass and silage production and cattle grazing  
128 since drainage in the 1920s (Kasimir Klemedtsson et al., 2009), whereas Örke was drained in  
129 1938 and is now under permanent pasture (McAfee, 1985). The Majnegården site has a layered  
130 structure with a highly decomposed plough layer down to about 25 cm depth (with mineral  
131 material and shells) and poorly decomposed soil below that, the peat being mainly reed peat  
132 (Berglund and Berglund, 2011). The peat at the Örke site is mainly a sedge-brown moss peat and  
133 is highly decomposed, but with low mineral matter content (Berglund and Berglund, 2011). The  
134 porosity of the topsoil at Majnegården is lower than at Örke, but soil water content at 40 cm and  
135 80 cm drainage depth is similar in both soils, which results in a higher proportion of air-filled  
136 pores in the profile at Örke at these drainage depths (Berglund and Berglund, 2011).

## 137 **1.2 Soil samples**

138 Undisturbed and disturbed (manufactured) peat samples were collected from the Pelso study  
139 sites. The undisturbed, moderately decomposed (approximately H4-H6 on von Post scale)  
140 samples were taken in sharpened PVC pipes (volume 1100 cm<sup>3</sup>, inner diameter 10 cm, height  
141 12-13 cm). Eight samples were taken from the peat extraction site (4 samples from 2-15 cm  
142 depth, 4 samples from 42-55 cm depth) and eight from the peatland forest (from 2-28 cm depth  
143 after removal of vegetation and an undecomposed moss layer), where the soil was pure peat with  
144 no added mineral matter. These samples had low mineral matter content (L samples). Sixteen  
145 undisturbed peat samples were also taken from the plough layer (2-15 cm) of the cultivated *Carex*  
146 peat site and these samples had medium mineral matter content (M samples). To increase the  
147 range of organic matter contents, an additional 16 samples were manufactured by mixing peat  
148 from the peat extraction site (from depth 0-70 cm) at its water content with mineral soil (particle  
149 size <2 mm, particle density 2.7 g cm<sup>-3</sup>) using a peat:mineral soil mass ratio of 1:0.6. The samples  
150 were compacted by hand. These samples had high mineral matter content (H samples).

151 All 48 samples of Pelso peat were drained to different water contents by a pressure plate device  
152 (e.g. Laurén and Heiskanen, 1997, Ronkanen and Kløve, 2005), with the pressure maintained for  
153 at least 7 days. After that time, a few drops of water were still leaving the samples but most of  
154 the water extractable by this method had been removed. Therefore, the water content reached  
155 was considered a close enough approximation of the true equilibrium water content  
156 corresponding to the matric potential in question. Four different moisture levels were created:  
157 fully saturated samples and samples with water content corresponding approximately to matric  
158 potential of -10 kPa, -40 kPa (only for L and M samples) and -500 kPa, which correspond to -  
159 100 cm, -400 cm and -5000 cm of water column, respectively. The final volumetric water content  
160 (VWC) range at saturated, -10 kPa, -40 kPa and -500 kPa matric potential was 0.67-0.90, 0.57-  
161 0.86, 0.62-0.76 and 0.46-0.72 m<sup>3</sup> m<sup>-3</sup>, respectively. Drainage in the pressure chamber caused the  
162 samples to shrink (median 10%, max. 18%), although the H samples shrank considerably only

163 at -500 kPa matric potential. For M samples, shrinkage at -10 kPa level was not measured.  
164 Shrinkage of samples was accounted for in the calculations by taking the reduced sample volume  
165 as total volume of the sample and assuming that the reduction was due to a decrease in pore  
166 volume. When the samples were frozen at -10°C, about 10-20% of the water was still unfrozen.  
167 However, there is some uncertainty associated with this estimate, which is based on the  
168 difference in VWC measured in the frozen state (using sensors) and the unfrozen state (calculated  
169 from oven drying), due to sensor error and the fact that the value calculated from oven drying  
170 was for the whole samples, whereas the sensors did not reach the lowest part of the samples.  
171 Despite this uncertainty, the peat samples could not be assumed to be fully frozen at temperatures  
172 close to 0°C.

173 Undisturbed samples from the 10-20 cm and 30-40 cm soil horizons at Majnegården and Örke  
174 were drained using the sand box method (Andersson, 1955), to a water content equivalent to  
175 drainage depth of 0.05 m, 0.4 m and 0.8 m (equivalent to -0.5, -4 and -8 kPa). When estimating  
176 thermal conductivity for these samples using models, porosity and VWC values estimated for  
177 each site and soil horizon based on Berglund et al. (2010) were used (Table 1). For the samples  
178 representing drainage of 0.05 m, VWC was calculated from porosity by assuming a water-filled  
179 pore space (WFPS) of 98%. Mass of solids ( $m_{\text{solids}}$ ) was calculated as product of BD and sample  
180 volume. Mass of mineral matter fraction ( $m_m$ ) was calculated as product of mineral matter  
181 content (1-OM) and  $m_{\text{solids}}$ . The volume of mineral matter fraction was calculated as product of  
182  $m_m$  and estimated particle density for mineral soil (2.7 g/cm<sup>3</sup> (de Vries, 1963)).

183

184 Table 1. Soil porosity, volumetric water content (VWC) and water-filled pore space (WFPS) in  
185 samples from the 10-20 cm and 30-40 cm soil layers at the Majnegården and Örke sites,  
186 estimated based on Berglund et al. (2010) and additional material.

| Majnegården

| Örke

| soil depth (cm) | drainage treatment group (m) | Porosity ( $\text{m}^3 \text{ m}^{-3}$ ) | VWC ( $\text{m}^3 \text{ m}^{-3}$ ) | WFPS ( $\text{m}^3 \text{ m}^{-3}$ ) | Porosity ( $\text{m}^3 \text{ m}^{-3}$ ) | VWC ( $\text{m}^3 \text{ m}^{-3}$ ) | WFPS ( $\text{m}^3 \text{ m}^{-3}$ ) |
|-----------------|------------------------------|--|-------------------------------------|--------------------------------------|--|-------------------------------------|--------------------------------------|
| 10-20           | 0.05                         | 0.69                                     | 0.68                                | 0.98                                 | 0.81                                     | 0.79                                | 0.98                                 |
|                 | 0.4                          | 0.69                                     | 0.63                                | 0.91                                 | 0.81                                     | 0.69                                | 0.85                                 |
|                 | 0.8                          | 0.69                                     | 0.60                                | 0.87                                 | 0.81                                     | 0.66                                | 0.82                                 |
| 30-40           | 0.05                         | 0.88                                     | 0.87                                | 0.98                                 | 0.86                                     | 0.84                                | 0.98                                 |
|                 | 0.4                          | 0.88                                     | 0.85                                | 0.96                                 | 0.86                                     | 0.76                                | 0.89                                 |
|                 | 0.8                          | 0.88                                     | 0.82                                | 0.93                                 | 0.86                                     | 0.73                                | 0.85                                 |

187

### 188 **1.3 Measurement of thermal conductivity**

189 The undisturbed and disturbed samples from Pelso were wrapped tightly in three layers of plastic  
190 sheeting, fitted into water-tight plastic containers and placed in a LAUDA RK 20 KS Compact  
191 Low-Temperature Thermostat chamber (filled with circulating antifreeze liquid) to reach the  
192 desired temperature. Thermal conductivity was measured at +1°C, -3°C, -5°C and -10°C and,  
193 for the L samples and M samples, also at +10°C. Each measurement was performed on four  
194 replicate samples, but in some cases results from only 2-4 samples were included in the analysis,  
195 due to indications of measurement errors (such as probe malfunction). To eliminate an initially  
196 observed vertical temperature gradient in the samples, the samples (other than M samples in  
197 saturated state and at -10 kPa and -40 kPa matric potential) were covered with additional  
198 insulating material before temperature measurement. However, the problem was not entirely  
199 removed, as a temperature difference of 1.5°C was observed between the top of the sample and  
200 9 cm depth. Thermal conductivity was measured using the single probe method (Farouki, 1986,  
201 Laurén, 1999), with probe length 7.5-10 cm (diameter 3 mm), heating time 15 min, resistor wire

202 resistance 11.5-33.7 ohms and current 0.04-0.15 mA (Fig. 1). The temperature change was kept  
203 as less than 2°C by adjusting the current to prevent the melting. We did observe regions of slower  
204 increase of temperature in response to heating in temperature curves (which would have  
205 indicated melting) in some measurement, and these measurements were excluded. The mean of  
206 2-3 successful measurements was used as the final  $\lambda$  value for each sample at the given water  
207 content. During the measuring sequence, soil temperature was monitored with a K-type wire  
208 connected to a Beamex Precision Thermometer TC-301, while VWC was measured with a  
209 Decagon EC-H2O Soil Moisture Sensor EC-5 probe calibrated for this type of peat soil. Soil  
210 VWC was also determined by drying the samples at 65°C (this temperature was chosen to avoid  
211 charring and the sample mass was carefully monitored until it stopped decreasing). OM was  
212 determined by incineration at 550°C (two replicates). Volumetric ice content was calculated as  
213 the difference in VWC measured in the frozen state (using Soil Moisture Sensor) and the  
214 unfrozen state (calculated from oven drying).

215 The thermal conductivity of the samples from Majnegården and Örke was measured at +20°C  
216 and -11°C (mean of 1-2 replicate measurements per sample, 1-3 samples per soil  
217 horizon/drainage level/temperature combination), using similar methods as for the Pelso  
218 samples, except that the temperature of -11°C was achieved using a freezer.

219

#### 220 **1.4 Models for estimating thermal conductivity**

221

222 Three well-known empirical models for determining the thermal conductivity of unfrozen peat  
223 were tested using the measured data from peat samples collected in this study. These were the de  
224 Vries (1963) model, the Dissanayaka et al. (2012) model and the Brovka and Rovdan (1999)  
225 model. The constants used in this study are presented in Table 2.

226

227 Model 1: The classic empirical model for calculating the thermal conductivity of organic soil  
 228 developed by de Vries (1963) (valid for volumetric air content  $VAC < 0.50 \text{ m}^3 \text{ m}^{-3}$ ):

$$229 \quad \lambda = (\theta \cdot \lambda_{\text{water}} + k_o \cdot \sigma_o \cdot \lambda_o + k_m \cdot \sigma_m \cdot \lambda_m + k_a \cdot \varepsilon \cdot \lambda_{\text{app}}) / (\theta + k_o \cdot \sigma_o + k_m \cdot \sigma_m + k_a \cdot \varepsilon) \quad (1)$$

230

231 where

232  $\theta$  = water fraction ( $\text{m}^3 \text{ m}^{-3}$ )

233  $\sigma_o$  = organic matter fraction ( $\text{m}^3 \text{ m}^{-3}$ )

234  $\sigma_m$  = mineral soil fraction ( $\text{m}^3 \text{ m}^{-3}$ )

235  $\varepsilon$  = air fraction ( $\text{m}^3 \text{ m}^{-3}$ )

236  $k_o$  = organic phase weight factor calculated with Eq. 2

237  $k_m$  = mineral soil phase weight factor calculated with Eq. 3

238  $k_a$  = air phase weight factor calculated with Eq. 4

239

$$240 \quad k_o = \frac{1}{3} \sum_{i=a,b,c} \left[ 1 + \left[ \frac{\lambda_o}{\lambda_{\text{water}}} - 1 \right] g_i \right]^{-1} \quad (2)$$

$$241 \quad k_m = \frac{1}{3} \sum_{i=a,b,c} \left[ 1 + \left[ \frac{\lambda_m}{\lambda_{\text{water}}} - 1 \right] g_i \right]^{-1} \quad (3)$$

242

$$243 \quad k_a = \frac{1}{3} \sum_{i=a,b,c} \left[ 1 + \left[ \frac{\lambda_{\text{app}}}{\lambda_{\text{water}}} - 1 \right] g_i \right]^{-1} \quad (4)$$

244

245 Model 2: An empirical model for estimating  $\lambda$  of peat by Dissanayaka et al. (2012) (Eq. 5).

246

$$247 \quad \lambda = 0.225 \cdot \sigma + 0.025 + 0.89 \cdot \lambda_{\text{water}} \cdot \theta \quad (5)$$

248

249 where  $\sigma$  = fraction of soil solids ( $\text{m}^3 \text{ m}^{-3}$ ).

250

251 Model 3: An empirical model developed by Brovka and Rovdan (1999), which is valid for peat-  
252 sand mixtures with less than 0.96 % by weight of sand.

253

$$254 \quad \lambda = a_0 + a_1 \cdot x_{\text{water}} + a_2 \cdot x_{\text{sand}} \cdot x_{\text{peat}} + a_3 \cdot x_{\text{sand}} \cdot x_{\text{water}} + a_4 \cdot x_{\text{sand}}^2 + a_5 \cdot x_{\text{peat}}^2 + a_6 \cdot x_{\text{water}}^2 \quad (6)$$

255

256 where

257  $x_{\text{water}}$  = % (by weight) of water in unfrozen sample

258  $x_{\text{sand}}$  = % (by weight) of sand in unfrozen sample

259  $x_{\text{peat}}$  = % (by weight) of peat in unfrozen sample.

260

261 In the present study, this model was tested both for unfrozen and frozen samples. The % (by  
262 weight) of sand ( $x_{\text{sand}}$ ) was approximated to equal sample ash content.

263

264

265

266

267 Table 2. Parameters used in the de Vries model (Eqs. 1-4) and model constant values given by  
 268 de Vries (1963)<sup>a</sup> and Brovka & Brovdan (1999)<sup>b</sup>.

| Symbol                              | Constants  | Value  | Note                                    |
|-------------------------------------|--|--|---|
| $\lambda_{\text{water}}^{\text{a}}$ | Thermal conductivity of water                          | 0.57 W m <sup>-1</sup> K <sup>-1</sup>   |   |
| $\lambda_{\text{o}}^{\text{a}}$     | Thermal conductivity of organic matter                 | 0.25 W m <sup>-1</sup> K <sup>-1</sup>   |   |
| $\lambda_{\text{m}}^{\text{a}}$     | Thermal conductivity of mineral soil                   | 2.9 W m <sup>-1</sup> K <sup>-1</sup><br>8.8 W m <sup>-1</sup> K <sup>-1</sup> | for clay<br>for quartz                  |
| $\lambda_{\text{app}}^{\text{a}}$   | Apparent thermal conductivity of gas-filled pore space | 0.05 W m <sup>-1</sup> K <sup>-1</sup>   | for air with water vapour               |
| $g_{\text{a}}^{\text{a}}$           | Particle shape factor                                  | 0.5  | assumes cylindrical soil particle shape |
| $g_{\text{b}}^{\text{a}}$           | Particle shape factor                                  | 0.5  | assumes cylindrical soil particle shape |
| $g_{\text{c}}^{\text{a}}$           | Particle shape factor                                  | 0  | assumes cylindrical soil particle shape |
| $a_0^{\text{b}}$                    | Empirical constant                                     | 1.98·10 <sup>-2</sup><br>2.38·10 <sup>-2</sup>                                 | unfrozen soil<br>frozen soil            |
| $a_1^{\text{b}}$                    | Empirical constant                                     | 6.56·10 <sup>-4</sup><br>5.37·10 <sup>-4</sup>                                 | unfrozen soil<br>frozen soil            |
| $a_2^{\text{b}}$                    | Empirical constant                                     | -1.22·10 <sup>-6</sup><br>-3.47·10 <sup>-6</sup>                               | unfrozen soil<br>frozen soil            |
| $a_3^{\text{b}}$                    | Empirical constant                                     | 8.69·10 <sup>-7</sup><br>2.75·10 <sup>-6</sup>                                 | unfrozen soil<br>frozen soil            |
| $a_4^{\text{b}}$                    | Empirical constant                                     | 6.43·10 <sup>-7</sup><br>8.81·10 <sup>-7</sup>                                 | unfrozen soil<br>frozen soil            |
| $a_5^{\text{b}}$                    | Empirical constant                                     | 2.11·10 <sup>-7</sup><br>2.04·10 <sup>-7</sup>                                 | unfrozen soil<br>frozen soil            |
| $a_6^{\text{b}}$                    | Empirical constant                                     | -1.24·10 <sup>-7</sup><br>1.71·10 <sup>-6</sup>                                | unfrozen soil<br>frozen soil            |

269

## 270 1.5 Analysis of thermal conductivity data

271 All data analysis was performed with R-software (version 3.4.2). The statistical testing was  
 272 performed using a mixed model (lme-function from nlme-package; Pinheiro et al., 2017), with  
 273 individual sample (sample\_id) as random effect (random intercept) using Restricted Maximum  
 274 Likelihood (REML). Analysis was performed separately for the frozen and unfrozen samples.  
 275 The thermal conductivity was log-transformed, based on model diagnostics suggesting non-  
 276 normality of residuals and heteroscedasticity of residual variances without transformation.

277 Overall significance of variable effects was determined by comparing models with and without  
278 variable effects. Comparison of models was based on likelihood ratios (by setting up alternative  
279 models using maximum likelihood instead of REML and then using the `anova.lme` command).

280 The individual models used in data analysis are shown in Appendix A.

281

282 The performance of thermal conductivity models by de Vries (1963) and Brovka and Brovdan  
283 (1999) and Dissanayaka et al. (2012) was compared using Lin's (1989, 2000) concordance  
284 correlation coefficient (CCC) (`epiR`-package; Nunes et al., 2018).

285

## 286 **2 Results and Discussion**

### 287 **2.1 Observed physical characteristics of the peat samples**

288 Physical properties of the peat depended on sampling site: samples from the plough layer of the  
289 Pelso cultivated site differed clearly from the non-cultivated peat samples. This was expected,  
290 since cultivation changes the porosity and bulk density (BD) of the plough layer. The main  
291 reasons are that peat is compacted due to the effect of mineralisation, physical ploughing and  
292 addition of mineral soil (Kechavarzi et al., 2010, McLay et al., 1992, Myllys and Soini, 2008).  
293 The L samples (pure peat) had the highest organic matter (lowest mineral matter) content  
294 (median OM content  $0.97 \text{ g g}^{-1}$ ) (Table 3). The M samples (from the plough layer of the cultivated  
295 peat site) had clearly lower median OM content (median  $0.56 \text{ g g}^{-1}$ ) due to cultivation practices,  
296 while the H samples (manufactured peat-sand mixture) had the lowest OM content (median  $0.17$   
297  $\text{g g}^{-1}$ ). However, estimated OM content was quite similar for all three groups of samples (Fig. 2).  
298 The L samples had the highest porosity and lowest BD, while the H samples had the lowest  
299 porosity and highest BD (Table 3). The organic matter content of the M samples were similar to  
300 that in both soil layers of the Majnegården peat (Table 3). The soil at Örke is highly decomposed  
301 but has a low mineral soil content, and thus more resembled L samples. As expected, VWC  
302 decreased with increasing matric potential. The H samples (manufactured peat-sand mixture)  
303 were drier than the M and L samples when saturated or at  $-10 \text{ kPa}$  matric potential, but VWC  
304 was more similar across sample groups at  $-500 \text{ kPa}$  (Fig. 2, Fig. 3).

305

306 Table 3. Median values (min-max) of soil properties of Pelso samples with high (H), medium  
 307 (M) and low (L) mineral matter content and of the 0-20 cm and 30-40 cm soil horizons at  
 308 Majnegården and Örke (Berglund and Berglund, 2011). n = number of replicate samples

| Soil sample group             | Porosity (m m <sup>-3</sup> ) | n | Organic matter content (g g <sup>-1</sup> ) | n  | Bulk density (g cm <sup>-3</sup> ) | n | Degree of decomposition (H1–H10 von Post scale) |
|-------------------------------|-------------------------------|---|---|----|------------------------------------|---|---|
| Samples from Pelso area       |                               |   |   |    |                                    |   |   |
| L                             | 0.86<br>(0.84–0.90)           | 4 | 0.97<br>(0.93–0.98)                         | 16 | 0.18<br>(0.14–0.22)                | 4 | H4–6  |
| M                             | 0.77<br>(0.74–0.80)           | 3 | 0.56<br>(0.23–0.66)                         | 19 | 0.34<br>(0.33–0.37)                | 3 | H4  |
| H                             | 0.67<br>(0.67–0.68)           | 3 | 0.17<br>(0.11–0.31)                         | 10 | 0.62<br>(0.60–0.65)                | 3 | na  |
| Samples from Majnegården site |                               |   |   |    |                                    |   |   |
| 0-10 cm                       | 0.69<br>(0.68-0.71)           | 4 | 0.64<br>(0.62-0.64)                         | 16 | 0.64<br>(0.60-0.66)                | 4 | H7–8  |
| 30–40 cm                      | 0.88<br>(0.88-0.89)           | 4 | 0.76<br>(0.75-0.80)                         | 8  | 0.21<br>(0.19-0.22)                | 4 | H1–2  |
| Samples from Örke site        |                               |   |   |    |                                    |   |   |
| 5-15 cm                       | 0.81<br>(0.80-0.82)           | 4 | 0.86<br>(0.84-0.86)                         | 34 | 0.31<br>(0.28-0.33)                | 4 | H9–10   |
| 30–40 cm                      | 0.86<br>(0.85-0.87)           | 4 | 0.87<br>(0.84-0.89)                         | 34 | 0.23<br>(0.21-0.23)                | 4 | H8–9  |

na = data not available. Note that OM values for the Pelso samples include all values determined for these samples, including samples for which thermal conductivity readings were discarded.

309

## 310 2.2 Observed thermal conductivities

311 Peat decomposition or sand addition to the topsoil layer increases the mineral matter content of  
 312 the peat. Higher mineral matter content was expected to result in higher thermal conductivity  
 313 (Konovalov and Roman, 1973, Brovka and Rovdan, 1999). The highest  $\lambda$  values for unfrozen  
 314 samples (median 0.85 W m<sup>-1</sup> K<sup>-1</sup>) were indeed found for the H samples with the highest mineral  
 315 matter content. However, the unfrozen thermal conductivity of the undisturbed M and L samples  
 316 did not differ substantially (median 0.58 W m<sup>-1</sup> K<sup>-1</sup> and 0.52 W m<sup>-1</sup> K<sup>-1</sup>, respectively) (Table 4).  
 317 The undisturbed samples of cultivated peat from Majnegården and Örke had the lowest unfrozen  
 318  $\lambda$  values. Overall, the measured  $\lambda$  values were similar to literature values reported for peat, which

319 are generally within the range 0.2-0.8 W m<sup>-1</sup> K<sup>-1</sup> (Brovka and Rovdan, 1999, Kettridge and Baird,  
320 2007, Kujala et al., 2008, Hamamoto et al., 2010).

321 The  $\lambda$  values obtained for frozen samples had high variation but had median values  
322 of 1.5 W m<sup>-1</sup> K<sup>-1</sup>, 1.5 W m<sup>-1</sup> K<sup>-1</sup> and 1.2 W m<sup>-1</sup> K<sup>-1</sup> for the H samples, M samples and L samples,  
323 respectively. In frozen state, the Majnegården and Örke samples showed  $\lambda$  values of 0.84-1.4 W  
324 m<sup>-1</sup> K<sup>-1</sup> (Table 5). The maximum observed values were somewhat higher than those reported in  
325 previous studies, which have generally been within the range 0.2-2.0 W m<sup>-1</sup> K<sup>-1</sup> (Konovalov and  
326 Roman, 1973, Brovka and Rovdan, 1999, Kujala et al., 2008), depending on mineral matter  
327 content and water content. This is likely because the VWC of the samples in this study was quite  
328 high, so the ice content of the frozen samples was also high (note that  $\lambda_{\text{ice}}$  is 2.2 W m<sup>-1</sup> K<sup>-1</sup>,  $\lambda_{\text{water}}$   
329 is 0.567 W m<sup>-1</sup> K<sup>-1</sup> and  $\lambda_{\text{air}}$  is 0.024 W m<sup>-1</sup> K<sup>-1</sup>).

330 Table 4. Median thermal conductivity ( $W m^{-1} K^{-1}$ , minimum and maximum in brackets) at  
 331 different matric potential values of unfrozen ( $T = +1^{\circ}C$ ) and frozen ( $T = -10^{\circ}C$ ) Pelso peat  
 332 samples with high (H), medium (M) and low (L) mineral content. n = number of replicate  
 333 samples.

| measurement conditions                       | L           | n | M           | n | H           | n   |
|--|-------------|---|-------------|---|-------------|-----|
| Unfrozen condition at $T = +1^{\circ}C$      |             |   |             |   |             | 334 |
| Saturated                                    | 0.54        | 4 | 0.66        | 3 | 0.92        | 336 |
|  | (0.50–0.60) |   | (0.63–0.74) |   | (0.88–1.4)  | 337 |
| -10 kPa                                      | 0.50        | 4 | 0.61        | 3 | 0.87        | 4   |
|  | (0.34–0.60) |   | (0.52–0.64) |   | (0.79–1.0)  | 338 |
| -40 kPa                                      | 0.49        | 4 | 0.42        | 3 | na          | 339 |
|  | (0.30–0.58) |   | (0.38–0.49) |   |             |     |
| -500 kPa                                     | 0.38        | 4 | 0.52        | 4 | 0.61        | 340 |
|  | (0.22–0.54) |   | (0.49–0.55) |   | (0.56–0.62) | 341 |
| Fully frozen condition at $T = -10^{\circ}C$ |             |   |             |   |             | 342 |
| Saturated                                    | 1.7         | 4 | 2.3         | 3 | 2.3         | 343 |
|  | (1.6–2.2)   |   | (1.6–2.4)   |   | (2.0–2.4)   | 344 |
| -10 kPa                                      | 1.5         | 4 | 1.6         | 3 | 1.5         | 4   |
|  | (0.68–1.6)  |   | (1.2–1.9)   |   | (1.3–1.7)   | 345 |
| -40 kPa                                      | 1.2         | 4 | 0.50        | 3 | na          | 346 |
|  | (0.64–1.5)  |   | (0.35–0.66) |   |             |     |
| -500 kPa                                     | 0.49        | 4 | 1.1         | 4 | 1.0         | 347 |
|  | (0.33–1.1)  |   | (0.80–1.2)  |   | (0.67–1.1)  |     |

348 Table 5. Thermal conductivity ( $\lambda$ ,  $W m^{-1} K^{-1}$ ) of peat samples from Majnegården and Örke at  
 349 different soil horizon, temperature and drainage levels. Values shown are mean of 1-3 samples  
 350 at each soil horizon/temperature/drainage level. Drainage depth of 0.05 m, 0.4 m and 0.8 m are  
 351 equivalent to -0.5, -4 and -8 kPa.

| Drainage depth (m)                                | Majnegården |          | Örke     |          |
|---|-------------|----------|----------|----------|
|   | 10-20 cm    | 30-40 cm | 10-20 cm | 30-40 cm |
| $\lambda$ ( $W m^{-1} K^{-1}$ ) at $+20^{\circ}C$ |             |          |          |          |
| 0.05  | 0.53        | 0.49     | 0.48     | 0.48     |
| 0.4   | 0.50        | 0.49     | 0.43     | 0.45     |
| 0.8   | 0.51        | 0.54     | 0.42     | 0.45     |
| $\lambda$ ( $W m^{-1} K^{-1}$ ) at $-11^{\circ}C$ |             |          |          |          |
| 0.05  | 1.2         | 1.4      | 1.1      | 1.1      |
| 0.4   | 1.1         | 1.1      | 0.84     | 0.89     |
| 0.8   | 1.0         | 1.3      | 0.84     | 0.88     |

## 353 **2.3 Effect of soil characteristics on thermal conductivity**

### 354 **2.3.1 Drainage level did not fully explain the differences in observed thermal** 355 **conductivities**

356 The M and H samples had significantly higher unfrozen and frozen thermal conductivity than  
357 the L samples when temperature and matric potential treatment (representing drainage depth)  
358 were taken into account in the analysis (Appendix B). The sample group (L, M or H) was very  
359 significant in estimating unfrozen  $\lambda$  (likelihood ratio: 35.3,  $p < 0.0001$ ), but also in estimating  
360 frozen  $\lambda$  (likelihood ratio: 16.9,  $p = 0.0098$ ). The difference in frozen  $\lambda$  between M and H samples  
361 was very small, whereas the unfrozen  $\lambda$  of H samples was considerably higher than that of M  
362 samples (Appendix B). It should be noted that the difference between the M and L groups almost  
363 disappeared when the samples with -40 kPa matric potential treatment were included in the  
364 comparison (there was no data on group H for the -40 kPa matric potential treatment). This seems  
365 to be due to the M samples in this treatment having had unusually low thermal conductivity. The  
366 results indicate that the plough layer of cultivated peat soils should be considered as a separate  
367 layer when thermal content is used as parameter in physical models that use groundwater depth  
368 to estimate soil water content. However, under field conditions, plant water uptake, specific soil  
369 cover and weather conditions also regulate soil water content, in addition to groundwater depth,  
370 so these results cannot be directly applied in models that do not consider those factors.

### 371 **2.3.2 Group H samples had higher thermal conductivity after accounting for** 372 **VWC, VAC and VIC**

373 The H samples were found to have higher unfrozen  $\lambda$  than the M and L samples, which had  
374 similar values, after accounting for VWC, VAC and VIC (Appendix B, Fig. 4). The effect of  
375 VWC, VAC and VIC had to be excluded when estimating the effect of mineral matter content,  
376 as thermal conductivity correlated with VAC (Pearson correlation coefficient  $r = -0.54$ ) and, for

377 the frozen samples, with VIC ( $r=0.34$ ). These two variables were also correlated with each other  
378 ( $r=-0.57$ ), so distinguishing their individual effects was not possible. Within peat sample groups  
379 (L, M, H), there was also a correlation between  $\lambda$  and VWC ( $r = 0.57$  to  $0.77$ ).

380

381 Sample group was significant in estimating unfrozen  $\lambda$  with VAC and VWC included in the  
382 model (likelihood ratio: 17.9,  $p<0.0001$ ), but the sample group only had a weak significance for  
383 frozen  $\lambda$  (likelihood ratio: 6.9,  $p$ -value: 0.032). These findings agree with Brovka and Rovdan  
384 (1999), who showed that in unfrozen peat  $\lambda$  increases with sand content, but that in frozen  
385 samples the effect depends on soil water content. However, in the present study, M samples had  
386 somewhat lower frozen and unfrozen  $\lambda$  than L samples after accounting for VWC, VAC and VIC  
387 (Appendix B). This may be due to the anomaly that the M samples which were treated at matric  
388 potential -40 kPa had very low  $\lambda$  values. The soil properties of this sub-group of M samples did  
389 not explain their low  $\lambda$  values. If the M samples at matric potential -40 kPa were excluded from  
390 the analysis, the M samples had somewhat higher  $\lambda$  than the L samples (Appendix B), the  
391 significance of sample group to model also decreasing slightly (likelihood ratio: 13.4,  $p$ =  
392 0.0012). The differences in porosity ranges observed in each sample group (H, M and L)  
393 introduce uncertainty to results as there is no data on  $\lambda$  for all combinations of VWC and VAC  
394 for each sample group. A study with more samples from different cultivated peat soils would  
395 increase the reliability of this result.

396

397 According to the model without the samples at -40 kPa, at average VWC and VAC the difference  
398 in unfrozen  $\lambda$  between H and L samples was around  $0.2 \text{ W m}^{-1} \text{ K}^{-1}$ , whereas difference in  
399 unfrozen  $\lambda$  between M and L samples was only around  $0.02 \text{ W m}^{-1} \text{ K}^{-1}$ . Similarly, the difference  
400 in frozen  $\lambda$  between H and L samples was around  $0.3 \text{ W m}^{-1} \text{ K}^{-1}$ , while between M and L samples  
401 it was only around  $0.07 \text{ W m}^{-1} \text{ K}^{-1}$ . Thus, it appears that when data are available on actual VWC

402 and porosity, the plough layer of cultivated peat soils should be considered as a separate layer in  
403 physical models only for the most mineral-soil enriched sites, while for most management  
404 planning purposes this is likely unnecessary.

405

## 406 **2.4 Ice content and frozen thermal conductivity increased slightly with** 407 **decreased temperature**

408 There was a statistically significant difference between frozen  $\lambda$  at  $-3^{\circ}\text{C}$ ,  $-5^{\circ}\text{C}$  and  $-10^{\circ}\text{C}$  when  
409 sample group, unfrozen sample VAC and unfrozen sample VWC were also accounted for  
410 (likelihood ratio: 9.4,  $p=0.0092$ ). However, the actual observed increase in  $\lambda$  from  $-3^{\circ}\text{C}$  to  $-10^{\circ}\text{C}$   
411 was not very large. For instance, for L samples with average unfrozen VAC and VWC, the  
412 increase was approximately from  $1.15 \text{ W m}^{-1} \text{ K}^{-1}$  to  $1.21 \text{ W m}^{-1} \text{ K}^{-1}$  (Appendix B). This change  
413 is likely due to increased ice content, e.g. the ice content in the average L sample would have  
414 increased approximately from  $0.45$  to  $0.49 \text{ m}^3 \text{ m}^{-3}$  (Appendix B). It appears that soil temperature  
415 difference between  $-3^{\circ}\text{C}$  and  $-10^{\circ}\text{C}$  does not need to be taken into account when estimating  
416 thermal conductivity of peat. However, it is important to consider that this observation only holds  
417 for temperatures lower than  $-3^{\circ}\text{C}$ , and in some peatland regions, e.g. in southern Sweden and  
418 southern Finland, the most common wintertime temperature even in topsoil may exceed  $-3^{\circ}\text{C}$ .  
419 For example, in a lysimeter study with undisturbed peat soil from Majnegården and Örke  
420 conducted at Ultuna in southern Sweden (Berglund and Berglund, 2011), soil temperature mainly  
421 stayed close to  $0^{\circ}\text{C}$  during the winter, indicating partial freezing in the topsoil (unpublished data).  
422 In that study, a decrease in VWC at 20 cm was observed only at the end of March and soil  
423 temperature at 20 cm depth did not drop below  $-3^{\circ}\text{C}$  at any point during the winter. In those  
424 conditions, the unfrozen water content of peat reached about  $0.40\text{-}0.50 \text{ m}^3 \text{ m}^{-3}$  in the field (in  
425 comparison, the unfrozen water content of the frozen Pelso samples at  $-10^{\circ}\text{C}$  was lower,  $0.10\text{-}$   
426  $0.20 \text{ m}^3 \text{ m}^{-3}$ ). For a region such as Ultuna the effect of sub-zero temperature on thermal  
427 conductivity is likely stronger than observed in this study and should not be ignored.

## 429 **2.5 De Vries model was best for estimating unfrozen thermal conductivity**

430 The mineral soil content of the samples affected the fit of the unfrozen peat  $\lambda$  models tested (Fig.  
431 5). All three models showed relatively good fit for samples with low mineral soil content (Table  
432 6). The classic de Vries model was the best predictor of  $\lambda$  for the L and M samples, while the  
433 Brovka-Rovdan model and especially the Dissanayaka et al. model underestimated  $\lambda$  for these  
434 samples (Fig. 5). The fit of the de Vries model for H samples was the best when the thermal  
435 conductivity of the mineral fraction ( $\lambda_m$ ) was assumed to be between the values for quartz sand  
436 and clay (Fig. 5). This also agrees with findings by Konovalov and Roman (1973) of different  
437 thermal conductivity in sandy peats than clayey peats. For the undisturbed samples in the present  
438 study (M samples and Majnegården plough layer samples), the fit of the de Vries model was  
439 much better with the lowest  $\lambda_m$  value tested ( $2.9 \text{ W m}^{-1} \text{ K}^{-1}$ , for clay). It appears that mineral  
440 matter type, if known, should be considered when using the de Vries model to estimate thermal  
441 conductivity for the plough layer of cultivated peat soils, especially when the mineral matter  
442 content is over 40 m-%, as observed in the disturbed samples in this study. The Dissanayaka et  
443 al. model, originally developed for pure peat samples, was the most sensitive to sand content in  
444 the soil and did not give a good fit to observations for M or H samples (Fig. 5, Table 6). The  
445 Brovka-Rovdan model, which assumes fully frozen soil, gave a reasonably good fit for all frozen  
446 samples (CCC = 0.58), although it had a tendency to overestimate the thermal conductivity of  
447 samples at lower soil water content (Fig. 6). The fit of the model was not markedly different  
448 across sub-zero temperatures. This indicates that while the ice content still changed as the  
449 temperature decreased from  $-3^\circ\text{C}$  to  $-10^\circ\text{C}$ , especially for the saturated samples with low mineral  
450 matter content, this did not affect soil thermal conductivity in a significant way.

453 Table 6. Model fit (Concordance Correlation Coefficient) of the de Vries, Brovka & Rovdan and  
 454 Dissanayaka et al. models in estimating the thermal conductivity of Pelso peat soils with high  
 455 (H), medium (M) and low (L) mineral matter content and of Örke and Majnegården peat soil  
 456 layers.  $\lambda_m$  = thermal conductivity of mineral matter

| Model  | All samples | Low mineral matter content (L samples, Örke samples and Majnegården samples of 30-40 cm depth) | Medium mineral matter content (M samples, Majnegården samples of 10-20 cm depth) | High mineral matter content (H samples) |
|--|-------------|--|--|---|
| De Vries,<br>$\lambda_m = 5.6 \text{ W m}^{-1} \text{ K}^{-1}$ | 0.81        | 0.67   | 0.38   | 0.32                                    |
| De Vries,<br>$\lambda_m = 2.9 \text{ W m}^{-1} \text{ K}^{-1}$ | 0.70        | 0.67   | 0.38   | 0.22                                    |
| De Vries<br>$\lambda_m = 8.8 \text{ W m}^{-1} \text{ K}^{-1}$  | 0.71        | 0.67   | 0.17   | 0.15                                    |
| Brovka & Rovdan,<br>unfrozen samples                           | 0.69        | 0.60   | 0.33   | 0.24                                    |
| Brovka & Rovdan,<br>frozen samples                             | 0.58        | 0.59   | 0.46   | 0.51                                    |
| Dissanayaka et al.   | 0.08        | 0.58   | 0.14   | 0.04                                    |

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### 464 3 Conclusions

- 465 • Peat soil samples with the highest proportion of mineral matter had the highest thermal  
466 conductivity in unfrozen condition. The samples with the highest mineral soil content had  
467 the highest thermal conductivity even when considering volumetric air and water content.  
468 However, it seems that in most cases, this only needs to be considered when modelling  
469 cultivated peat soil with higher mineral matter content than the cultivated site sampled in  
470 this study. This study differed from most previous studies on thermal conductivity of peat  
471 by using undisturbed samples, but a wider study on thermal regimes of cultivated peat  
472 soil in field conditions would bring even more insight on the practical significance of the  
473 observed differences.
- 474 • Peat soil samples, especially pure peat, were not fully frozen at  $-3^{\circ}\text{C}$  and  $-5^{\circ}\text{C}$ , but this  
475 did not have a considerable effect on  $\lambda$  compared with that at  $-10^{\circ}\text{C}$ . However, this result  
476 does not necessarily apply for temperatures between  $-3^{\circ}\text{C}$  and  $0^{\circ}\text{C}$ . A study with different  
477 methodology is needed to establish how thermal conductivity of peat changes in that  
478 critical temperature range.
- 479 • The best model for predicting the thermal conductivity of unfrozen mineral soil-enriched  
480 peat was found to be the classic de Vries model. The Brovka-Rovdan model also  
481 performed reasonably well for frozen peat soils and for unfrozen peat soils with low  
482 mineral matter content.

483

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571

572

573

## Appendix A. R syntax of models used in the analysis

574 The effect of sample group (sample\_group) on thermal conductivity at different temperature  
575 (temperature\_group, levels: unfrozen, -3°C, -5°C, -10°C) and matric potentials  
576 (matric\_potential, levels: saturated, -10 kPa, -500 kPa) was examined with model m1.

577

578 The **full models** were m1.unfrozen.a and m1.frozen.a:

```
579 m1.unfrozen.a <- lme(log(thermal_conductivity)) ~ matric_potential* sample_group,
```

```
580 random = ~ 1|sample_id , ...,
```

```
581 method = "REML")
```

582

```
583 m1.frozen.a <- lme(log(thermal_conductivity)) ~ temperature_group*matric_potential*
```

```
584 sample_group,
```

```
585 random = ~ 1|sample_id , ...,
```

```
586 method = "REML")
```

587

588 The **final models** with significant effects were m1.unfrozen.b and m1.frozen.b:

```
589 m1.unfrozen.b <- lme(log(thermal_conductivity)) ~ matric_potential + sample_group,
```

```
590 random = ~ 1|sample_id , ...,
```

```
591 method = "REML")
```

592

```
593 m1.frozen.b <- lme(log(thermal_conductivity)) ~ matric_potential + sample_group,
```

```
594 random = ~ 1|sample_id , ...,
```

```
595 method = "REML")
```

596

597 The effect of sample group on thermal conductivity when standardized in respect to (centred)  
598 volumetric percentage of air (VAC), water (VWC) and ice (VIC; only for frozen samples) was  
599 examined with model m2.

600 The **full models** were m2.unfrozen.a and m2.frozen.a :

601

```
602 m2.unfrozen.a <- lme(log(thermal_conductivity)) ~ VAC*VWC + sample_group,
```

```
603 random = ~ 1|sample_id, ...,
```

```
604 method = "REML")
```

605

```
606 m2.frozen.a <- lme(log(thermal_conductivity)) ~ VAC+ VWC + VIC + VAC:VIC + VAC:VWC
```

```
607 + VIC:VWC + sample_group,
```

```
608 random = ~ 1|sample_id, ...,
```

```
609 method = "REML")
```

610

611 The **final models** with significant effects were m2.unfrozen.b and m2.frozen.b:

612

```
613 m2.unfrozen.b <- lme(log(thermal_conductivity)) ~ VAC+ VWC + sample_group,
```

```
614 random = ~ 1|sample_id, ...,
```

```
615 method = "REML")
```

616

```
617 m2.frozen.b <- lme(log(thermal_conductivity)) ~ VAC+ VWC + VIC + VAC:VIC +
```

```
618 sample_group,
```

```
619 random = ~ 1|sample_id, ...,
```

```
620 method = "REML")
```

621

622 The effect of temperature on the thermal conductivity of frozen samples was examined with  
623 model m3.

624

```
625 m3 <- lme(log(thermal_conductivity)) ~ unfrozen_VAC+ unfrozen_VWC + sample_group,  
626 random = ~ 1|sample_id, ...,  
627 method = "REML")
```

628

629 The effect of temperature on ice content was examined with model m4.

630

```
631 m4 <- lme(VIC ~ unfrozen_VAC+ unfrozen_VWC + sample_group,  
632 random = ~ 1|sample_id, ...,  
633 method = "REML")
```

634

635

## Appendix B. Model summary tables

636 The models are defined in Appendix A. SE = Standard Error, df= degree of freedom

637 Model m1.unfrozen.b

|                           | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|---------------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)               | -0.738       | 0.0663    | 125       | -11.1          | <0.001         |
| matric_potential-500kPa   | -0.213       | 0.075     | 27        | -2.84          | 0.00839        |
| matric_potentialSaturated | 0.143        | 0.0769    | 27        | 1.86           | 0.0737         |
| sample_groupHigh          | 0.556        | 0.0762    | 27        | 7.29           | <0.001         |
| sample_groupMedium        | 0.277        | 0.0741    | 27        | 3.74           | <0.001         |

638

639 Model m1.frozen.b

|                           | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|---------------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)               | 0.1          | 0.0999    | 249       | 1              | 0.317          |
| matric_potential-500kPa   | -0.606       | 0.112     | 27        | -5.4           | <0.001         |
| matric_potentialSaturated | 0.314        | 0.115     | 27        | 2.73           | 0.0109         |
| sample_groupHigh          | 0.343        | 0.112     | 27        | 3.05           | 0.00513        |
| sample_groupMedium        | 0.338        | 0.112     | 27        | 3.01           | 0.00565        |

640

641

642 Model m2.unfrozen.b

|                    | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|--------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)        | -0.653       | 0.0814    | 160       | -8.03          | <0.001         |
| VWC_centred        | -0.0101      | 0.01      | 34        | -1.01          | 0.321          |
| VAC_centred        | -0.0289      | 0.0102    | 34        | -2.83          | 0.00769        |
| sample_groupHigh   | 0.321        | 0.196     | 34        | 1.64           | 0.11           |
| sample_groupMedium | -0.0231      | 0.134     | 34        | -0.173         | 0.864          |

643

644 Model m2.unfrozen.b, without samples in matric potential treatment group -40 kPa

|                    | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|--------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)        | -0.639       | 0.0856    | 125       | -7.46          | <0.001         |
| VWC_centred        | -0.0107      | 0.00976   | 27        | -1.09          | 0.284          |
| VAC_centred        | -0.0289      | 0.0102    | 27        | -2.82          | 0.00898        |
| sample_groupHigh   | 0.339        | 0.188     | 27        | 1.8            | 0.0824         |
| sample_groupMedium | 0.035        | 0.134     | 27        | 0.262          | 0.796          |

645

646

647 Model m2.frozen.b

|                         | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|-------------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)             | 0.146        | 0.193     | 299       | 0.757          | 0.45           |
| VWC_centred             | -0.0214      | 0.0214    | 299       | -0.999         | 0.319          |
| VAC_centred             | -0.0581      | 0.0213    | 299       | -2.73          | 0.00666        |
| VIC_centred             | -0.00863     | 0.0206    | 299       | -0.419         | 0.676          |
| sample_groupHigh        | 0.076        | 0.392     | 36        | 0.194          | 0.847          |
| sample_groupMedium      | -0.229       | 0.267     | 36        | -0.855         | 0.398          |
| VAC_centred:VIC_centred | -0.00039     | 0.000343  | 299       | -1.14          | 0.256          |

648

649

650

651 Model m2.unfrozen.b, without samples in the -40 kPa matric potential treatment.

|                         | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|-------------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)             | 0.0647       | 0.156     | 245       | 0.416          | 0.678          |
| VWC_centred             | -0.0213      | 0.0165    | 245       | -1.29          | 0.198          |
| VAC_centred             | -0.0564      | 0.0168    | 245       | -3.36          | <0.001         |
| VIC_centred             | -0.0059      | 0.0156    | 245       | -0.379         | 0.705          |
| sample_groupHigh        | 0.232        | 0.289     | 29        | 0.801          | 0.43           |
| sample_groupMedium      | 0.0629       | 0.207     | 29        | 0.304          | 0.763          |
| VAC_centred:VIC_centred | -0.00062     | 0.000322  | 245       | -1.94          | 0.0539         |

652

653

654 Model m3

|                      | <b>Value</b> | <b>SE</b> | <b>df</b> | <b>t-value</b> | <b>p-value</b> |
|----------------------|--------------|-----------|-----------|----------------|----------------|
| (Intercept)          | 0.194        | 0.184     | 301       | 1.05           | 0.293          |
| unfrozen_VWC_centred | -0.00528     | 0.0193    | 34        | -0.274         | 0.786          |
| unfrozen_VAC_centred | -0.0497      | 0.0196    | 34        | -2.53          | 0.016          |
| sample_groupHigh     | 0.113        | 0.376     | 34        | 0.3            | 0.766          |
| sample_groupMedium   | -0.228       | 0.257     | 34        | -0.886         | 0.382          |
| temperature-5        | -0.0529      | 0.021     | 301       | -2.52          | 0.0122         |
| temperature-3        | -0.0582      | 0.0209    | 301       | -2.78          | 0.00577        |

655

656

657 Model m4

|                      | <b>Value</b> | <b>SE</b> | <b>DF</b> | <b><i>t</i>-value</b> | <b><i>p</i>-value</b> |
|----------------------|--------------|-----------|-----------|-----------------------|-----------------------|
| (Intercept)          | 49.3         | 1.22      | 301       | 40.5                  | <0.001                |
| unfrozen_VWC_centred | 1.1          | 0.128     | 34        | 8.66                  | <0.001                |
| unfrozen_VAC_centred | 0.301        | 0.13      | 34        | 2.32                  | 0.0267                |
| sample_groupHigh     | 2.54         | 2.49      | 34        | 1.02                  | 0.315                 |
| sample_groupMedium   | -0.00267     | 1.7       | 34        | -0.00157              | 0.999                 |
| temperature-5        | -2.52        | 0.0856    | 301       | -29.4                 | <0.001                |
| temperature-3        | -4.52        | 0.0854    | 301       | -52.9                 | <0.001                |

658